

Natural Convection Correlations for Various Geometries

Highlights of this MathCAD formulations:

1. Uniform naming convention reduces probability of mistakes (different book have different symbols)
2. All the applicable range of Pr & Ra defined in function leading to foolproof functionality
3. Naming convention with respect of direction of gravity & hence absolute clarity in formulations
4. The lower limits of Pr has been reduced to 0.5 from 0.7 to handle all instances of Air
5. Formula checks by sample calculations after each formulation

Geometrical Dimension, Material Properties and Operating Conditions

$$Pr = 0.70$$

$$T_S = 100^\circ\text{C}$$

$$T_A = 40^\circ\text{C}$$

$$\beta = \frac{1}{T_A} = 3.193 \times 10^{-3} \frac{1}{\text{K}}$$

$$\nu = 18 \cdot 10^{-6} \frac{\text{m}^2}{\text{s}} \text{ at } [T_A + T_S]/2$$

$$L_c = 500\text{mm}$$

$$\theta = 0^\circ \quad \text{Vertical Plate}$$

$$Gr_{Lc} = \frac{g \cdot \beta \cdot (T_S - T_A) \cdot L_c^3}{\nu^2}$$

$$Ra_L = Gr_{Lc} \cdot Pr$$

$$\theta = \theta \quad \text{Inclined Plate}$$

$$\theta = 90^\circ \quad \text{Horizontal Plate}$$

Separate correlation

$$\text{Regime}(Gr_{Lc}) = \begin{cases} \text{"Laminar"} & \text{if } Gr_{Lc} < 10^9 \\ \text{"Turbulent"} & \text{otherwise} \end{cases}$$

$$\text{Regime}(Gr_{Lc}) = \text{"Laminar"}$$

Vertical Plate:

Applicable to V. Cylinder, if: $\frac{D}{L} > \frac{35}{Gr_L^{0.25}}$

$L_c = \text{Height of the Plate} = L$

Restrictions on Pr: **None**

$0^\circ < \theta < 60^\circ$: effect of tilt is not significant use $\theta = 0^\circ$.

$$Nu_{VPx}(Ra_L, \theta) = \begin{cases} 0.59 (Ra_L \cdot \cos(\theta))^{\frac{1}{4}} & \text{if } 10^4 < Ra_L \leq 10^9 \\ 0.14 (Ra_L \cdot \cos(\theta))^{\frac{1}{3}} & \text{if } 10^9 < Ra_L \leq 10^{13} \end{cases}$$

$$Nu_{vpX} = Nu_{VPx}(Ra_L, 30^\circ) = 85.4$$

$$Nu_{vpX1} = Nu_{VPx}(Ra_L, 0^\circ) = 88.6$$

$$Nu_{vpX2} = Nu_{VPx}(Ra_L, 75^\circ) = 63.2$$

Since both Nu and $Ra^{1/3}$ are proportional to L, for $Ra_L > 10^9$, the choice of L is immaterial.

Churchill and Chu (1975)

$$Nu_{VP}(Ra_L, \theta) = \begin{cases} \left[0.825 + \frac{0.387 \cdot (Ra_L \cdot \cos(\theta))^{\frac{1}{6}}}{\frac{8}{27}} \right]^2 & \text{if } 10^9 \leq Ra_L \leq 10^{12} \\ \left[0.68 + \frac{0.67 \cdot (Ra_L \cdot \cos(\theta))^{\frac{1}{4}}}{\frac{4}{9}} \right]^{\frac{9}{16}} & \text{if } 0.1 \leq Ra_L < 10^9 \end{cases}$$

$$Nu_{VPz} = Nu_{VP}(Ra_L, 75^\circ) = 55.6$$

$$Nu_{VPz1} = Nu_{VP}(Ra_L, 15^\circ) = 77.1$$

$$Nu_{VPz2} = Nu_{VP}(Ra_L, 45^\circ) = 71.3$$

Horizontal Plate:

*Upper side of Hot Plate (lower side insulated) /
Lower side of Cold Plate (upper side insulated)*

Lloyd and Moran (1974)

$$Nu_{HP1}(Ra_L) = \begin{cases} 0.96 Ra_L^{\frac{1}{3}} & \text{if } 1 < Ra_L \leq 200 \\ 0.59 Ra_L^{\frac{1}{4}} & \text{if } 200 < Ra_L \leq 2 \cdot 10^4 \\ 0.54 Ra_L^{\frac{1}{4}} & \text{if } 2.2 \cdot 10^4 < Ra_L \leq 8 \cdot 10^6 \\ 0.15 Ra_L^{\frac{1}{3}} & \text{if } 8 \cdot 10^6 < Ra_L \leq 10^{11} \end{cases}$$

*Lower side of Hot Plate (upper side insulated) /
Upper side of Cold Plate (lower side insulated)*

Lloyd and Moran (1974)

$$Nu_{HP2}(Ra_L) = \begin{cases} 0.27 Ra_L^{\frac{1}{4}} & \text{if } 10^4 \leq Ra_L \leq 10^{11} \\ \text{"Some variable is out of range!"} & \text{otherwise} \end{cases}$$

Lc = Area / Perimeter

Relative Benchmarking with Vertical Plate:

Width/Length of H. Plate = height of V. Plate

$$Lc_{HP} = \frac{Lc^2}{4 \cdot Lc} = 125 \cdot \text{mm}$$

Pr >= 0.7

$$Nu_{hp1} = Nu_{HP1} \left[Ra_L \cdot \left(\frac{Lc_{HP}}{Lc} \right)^3 \right] = 28.7$$

Pr >= 0.7

$$Nu_{hp2} = Nu_{HP2} \left[Ra_L \cdot \left(\frac{Lc_{HP}}{Lc} \right)^3 \right] = 14.3$$

HTC from plates hot or cold on both horizontal surfaces is average of the two correlations.

Horizontal Cylinder:

$$Nu_{HC}(Ra_D) = \left[0.60 + \frac{0.387 \cdot Ra_D^{\frac{1}{6}}}{\left[1 + \left(\frac{0.559}{Pr} \right)^{0.5625} \right]^{\frac{8}{27}}} \right]^2$$

Relative Benchmarking with Vertical Plate:
Cylinder with perimeter = Height of V. Plate

$$D_C = \frac{L_c}{\pi} = 0.159 \text{ m}$$

$$Nu_{hc} = Nu_{HC} \left[Ra_L \cdot \left(\frac{D_C}{L_c} \right)^3 \right] = 32.6$$

$$10^{-6} \leq Ra_D \leq 10^{12}$$

All Pr

Sphere:

$$Nu_{SPH}(Ra_D) = \left[2.0 + \frac{0.589 \cdot Ra_D^{0.25}}{\left[1 + \left(\frac{0.469}{Pr} \right)^{0.5625} \right]^{\frac{4}{9}}} \right]^{\frac{4}{9}}$$

Relative Benchmarking:
Sphere with perimeter = Height of V. Plate

$$D_S = \frac{L_c}{\pi} = 0.159 \text{ m}$$

$$Nu_{sph} = Nu_{SPH} \left[Ra_L \cdot \left(\frac{D_S}{L_c} \right)^3 \right] = 30.9$$

$$Ra_D \leq 10^{11}$$

$$Pr \geq 0.7$$

Vertical Iso-temperature Parallel Plates separated by distance 'S' - developing & fully developed:

For benchmarking with vertical plates, formulation of Ra-number in terms of L_c is maintained!

$$S_v = 500.0 \text{ mm} \leftarrow \text{Characteristic dimension for Ra}$$

$$Nu = h \cdot S/k$$

Bar-Cohen and Rohsenow (1984):

$$Nu_{VIP}(Ra_L) = \left[\frac{576}{\left[Ra_L \cdot \left(\frac{S_v}{L_c} \right)^3 \cdot \frac{S_v}{L_c} \right]^2} + \frac{2.83}{\left[Ra_L \cdot \left(\frac{S_v}{L_c} \right)^3 \cdot \frac{S_v}{L_c} \right]^{0.5}} \right]^{-\frac{1}{2}}$$

$$Ra_S = Ra_L \cdot \left(\frac{S_v}{L_c} \right)^3$$

$$Nu_{vip} = Nu_{VIP}(Ra_L) = 89.2$$

Vertical Symmetric Iso-flux Parallel Plates separated by distance 'S':

$$Nu_{VIF}(Ra_L) = \left[\frac{48}{\left[Ra_L \cdot \left(\frac{S_v}{L_c} \right)^3 \cdot \frac{S_v}{L_c} \right]^2} + \frac{2.51}{\left[Ra_L \cdot \left(\frac{S_v}{L_c} \right)^3 \cdot \frac{S_v}{L_c} \right]^{0.5}} \right]^{-\frac{1}{2}}$$

$$Nu_{vif} = Nu_{VIF}(Ra_L) = 94.7$$

Vertical Isothermal-Adiabatic Parallel Plates separated by distance 'S':

$$Nu_{IAD}(Ra_L) = \left[\frac{144}{\left[Ra_L \cdot \left(\frac{S_V}{L_c} \right)^3 \cdot \frac{S_V}{L_c} \right]^2} + \frac{2.87}{\left[Ra_L \cdot \left(\frac{S_V}{L_c} \right)^3 \cdot \frac{S_V}{L_c} \right]^{0.5}} \right]^{-\frac{1}{2}}$$

$$Nu_{iad} = Nu_{IAD}(Ra_L) = 88.6$$

Vertical Flux-Adiabatic Parallel Plates separated by distance 'S':

$$Nu_{FAD}(Ra_L) = \left[\frac{24}{\left[Ra_L \cdot \left(\frac{S_V}{L_c} \right)^3 \cdot \frac{S_V}{L_c} \right]^2} + \frac{2.51}{\left[Ra_L \cdot \left(\frac{S_V}{L_c} \right)^3 \cdot \frac{S_V}{L_c} \right]^{0.5}} \right]^{-\frac{1}{2}}$$

$$Nu_{fad} = Nu_{FAD}(Ra_L) = 94.7$$

Vertical Rectangular Enclosure, Dimension along gravity L_C perpendicular to gravity 'S':

$S_V = 500.0\text{mm}$ <- Characteristic dimension for Ra **Heated from sides, also called Tall Enclosures**

Berkovsky & Polevikov for aspect ratio (A.R.) up to 10 and MacGregor & Emery (1969) for A.R. > 10:

$$Nu_{VEN}(Ra_S, S, L) = \begin{cases} 0.18 \left(\frac{Pr}{0.2 + Pr} Ra_S \right)^{0.29} & \text{if } \frac{Pr \cdot Ra_S}{0.2 + Pr} \geq 1000 \wedge 1 \leq \frac{L}{S} \leq 2 \wedge 10^{-3} \leq Pr \leq 10^5 \\ 0.22 \left(\frac{Pr}{0.2 + Pr} Ra_S \right)^{0.28} \cdot \left(\frac{L}{S} \right)^{\frac{1}{4}} & \text{if } 10^3 \leq Ra_S \leq 10^{13} \wedge 2 < \frac{L}{S} \leq 10 \wedge Pr \leq 10^5 \\ 0.42 Ra_S^{\frac{1}{4}} \cdot Pr^{0.012} \cdot \left(\frac{L}{S} \right)^{\frac{1}{3}} & \text{if } 10^4 < Ra_S \leq 10^7 \wedge 10 < \frac{L}{S} \leq 40 \wedge 0.5 \leq Pr \leq 2 \cdot 10^4 \\ \text{"Variable(s) seems to be out of range!"} & \text{otherwise} \end{cases}$$

$$\frac{Pr \cdot \left[Ra_L \cdot \left(\frac{S_V}{L_c} \right)^3 \right]}{0.2 + Pr} = 3.9 \times 10^8 \quad Ra_L \cdot \left(\frac{S_V}{L_c} \right)^3 = 5.1 \times 10^8 \quad Nu_{ven} = Nu_{VEN} \left[Ra_L \cdot \left(\frac{S_V}{L_c} \right)^3, S_V, L_c \right] = 56$$

Inclined Rectangular Enclosure, Dimension along plates L_C perpendicular to plates 'S':

$\theta_H = 50^\circ$ $0^\circ < \theta_H \leq 70^\circ$ $\cos(\theta_H) = 0.643$

$$nZ(x) = \begin{cases} x & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases} \quad (\text{Hollands et al})$$

$$\text{Nu}_{\text{INC}}(\text{Ra}_S, S, L, \theta) = \begin{cases} 1 & \text{if } \text{Ra}_S \cdot \cos(\theta) \leq 1708 \wedge 12 \leq \frac{L}{S} \wedge 0^\circ < \theta \leq 70^\circ \\ \xi \leftarrow \left(1 - \frac{1708}{\text{Ra}_S \cdot \cos(\theta)} \right) \\ \psi \leftarrow 1 - \frac{1708 \cdot (\sin(1.8 \cdot \theta))^{1.6}}{\text{Ra}_S \cdot \cos(\theta)} \\ \zeta \leftarrow \frac{(\text{Ra}_S \cdot \cos(\theta))^{0.333}}{18} - 1 \\ 1 + 1.44 \text{nZ}(\xi) \cdot \text{nZ}(\psi) + \text{nZ}(\zeta) & \text{if } 1708 < \text{Ra}_S \leq 10^5 \wedge \frac{L}{S} \geq 12 \wedge 0^\circ < \theta \leq 70^\circ \\ \text{"Variable(s) seems to be out of range!"} & \text{otherwise} \end{cases}$$

$$\text{Ra}_L \cdot \left(\frac{S_V}{L_c} \right)^3 = 5.1 \times 10^8 \quad \text{Nu}_{\text{inc}} = \text{Nu}_{\text{INC}} \left[\text{Ra}_L \cdot \left(\frac{S_V}{L_c} \right)^3, S_V, L_c, \theta_H \right] = \text{"Variable(s) seems to be out of range!"}$$

Critical tilt angle after which the boundary layer will become thermally unstable.

Aspect Ratio = (1.0 3.0 6.0 12 $\theta > 12$) (Arnold et al - 1976)

Critical Tilt Angle = (155 127 120 113 110)

Inclined SQUARE Enclosure, tilt-angle with respect of horizontal direction:

For horizontal square enclosure, the heat transfer is solely by conduction and hence $\text{Nu}(0^\circ) = 1$

Horizontal Rectangular Enclosure, Dimension along gravity L_C perpendicular to gravity 'S':

Heated from Bottom, **expression for Nu applicable to Top surface**. Nu for bottom surface to be estimated from applied heat flux or indirectly from heat loss through the top surface. The aspect ratio "vertical height"/ "horizontal length" must be sufficiently high (~ 10 or more) to reduce effect of side-walls.

Note that the designation of geometrical parameter is same as vertical enclosure and hence refer to different "physically significant dimensions".

Jacob:

Also called Shallow Enclosures

$$\text{Nu}_{\text{JCB}}(\text{Ra}_L) = \begin{cases} 0.195 \text{Ra}_L^{\frac{1}{4}} & \text{if } 10^4 < \text{Ra}_L \leq 4 \cdot 10^5 \wedge 0.5 \leq \text{Pr} \leq 2.0 \\ 0.068 \text{Ra}_L^{\frac{1}{3}} & \text{if } 4 \cdot 10^5 < \text{Ra}_L \leq 10^9 \\ \text{"Variable(s) seems to be out of range!"} & \text{otherwise} \end{cases}$$

$$\text{Nu}_{\text{JCB}}(\text{Ra}_L) = 54.2$$

Globe and Dropkin (1959):

$$\text{Nu}_{\text{GLD}}(\text{Ra}_L) = \begin{cases} 0.069 \text{Ra}_L^{\frac{1}{3}} \cdot \text{Pr}^{0.074} & \text{if } 3 \cdot 10^5 < \text{Ra}_L \leq 7 \cdot 10^9 \\ \text{"Variable(s) seems to be out of range!"} & \text{otherwise} \end{cases}$$

$$\text{Nu}_{\text{GLD}}(\text{Ra}_L) = 53.6$$

Concentric Cylinders and Spheres:

$$L_C = (D_o - D_i) / 2$$

Raithby and Hollands (1975):

$$Q_{\text{ANN}}(T_i, T_o, D_i, D_o, k, \text{Ra}) = \begin{cases} F \leftarrow \frac{\left(\ln \left(\frac{D_o}{D_i} \right) \right)^4}{\left[\frac{(D_o - D_i)}{2} \right]^3 \cdot \left(\frac{1}{D_o^{0.6}} + \frac{1}{D_i^{0.6}} \right)^5} \\ k_E \leftarrow \left(\frac{\text{Pr}}{0.861 + \text{Pr}} \right)^{\frac{1}{4}} \cdot (\text{Ra} \cdot F)^{\frac{1}{4}} \\ \left[\frac{2 \cdot \pi \cdot (0.386 k \cdot k_E)}{\ln \left(\frac{D_o}{D_i} \right)} \cdot (T_i - T_o) \right] & \text{if } 0.5 \leq \text{Pr} \leq 6 \cdot 10^3 \wedge 10^2 \leq F \cdot \text{Ra} \leq 10^7 \\ \text{"Variable(s) seems to be out of range!"} & \text{otherwise} \end{cases}$$

For $F \cdot \text{Ra}_L < 100$, natural convection currents are negligible and the annular passage can be assumed to be static fluid that is $k_{EF} = k$. Also note that 2 Nu will need to be defined for inner and outer diameters.

$$T_i = T_S \quad T_o = T_A \quad k = 0.026 \frac{W}{m \cdot K}$$

$$D_i = 0.1m \quad D_o = 0.4m$$

Thermo-physical properties at $(T_i + T_o)/2$.

$$D_H = \frac{D_o - D_i}{2} = 150 \cdot mm$$

$$F_{ann} = \frac{\left(\ln \left(\frac{D_o}{D_i} \right) \right)^4}{\left[\frac{(D_o - D_i)}{2} \right]^3 \cdot \left(\frac{1}{D_o^{0.6}} + \frac{1}{D_i^{0.6}} \right)^5} = 0.18$$

$$Ra_{ann} = F_{ann} \cdot \left[Ra_L \cdot \left(\frac{D_o - D_i}{2 \cdot Lc} \right)^3 \right] = 2.5 \times 10^6$$

$$Q_{ann} = Q_{ANN}(T_i, T_o, D_i, D_o, k, Ra_{ann}) = 57.6 \cdot \frac{W}{m}$$

$$Ra_{Di} = Ra_L \cdot \left(\frac{D_i}{Lc} \right)^3 = 4.1 \times 10^6$$

Alternate formulation based on inner diameter of the annulus is:

$$q_{ANN}(T_i, T_o, D_i, D_o, k, Ra_{Di}) = \begin{cases} \frac{2.425 \cdot k \cdot (T_i - T_o)}{\left[1 + \left(\frac{D_i}{D_o} \right)^{0.6} \right]^{1.25}} \cdot \left(\frac{Pr \cdot Ra_{Di}}{0.861 + Pr} \right)^{\frac{1}{4}} & \text{if } 0.6 \leq Pr \leq 6000 \wedge Ra_{Di} \leq 10^7 \\ \text{"Variable(s) seems to be out of range"} & \text{otherwise} \end{cases}$$

$$q_{ann} = q_{ANN}(T_i, T_o, D_i, D_o, k, Ra_{Di}) = 88.5 \cdot \frac{W}{m}$$

Alternate formulation based on inner diameter of the **concentric spheres** is:

$$q_{ASP}(T_i, T_o, D_i, D_o, k, Ra_{Di}) = \begin{cases} \frac{2.325 \cdot k \cdot (T_i - T_o)}{\left[1 + \left(\frac{D_i}{D_o} \right)^{1.4} \right]^{1.25}} \cdot \left(\frac{Pr \cdot Ra_{Di}}{0.861 + Pr} \right)^{\frac{1}{4}} & \text{if } 0.6 \leq Pr \leq 4000 \wedge Ra_{Di} \leq 10^4 \\ \text{"Variable(s) seems to be out of range"} & \text{otherwise} \end{cases}$$

$$q_{asp} = q_{ASP}(T_i, T_o, D_i, D_o, k, Ra_{Di}) = \text{"Variable(s) seems to be out of range"} \cdot \frac{W}{m}$$

Optimum fin spacing for a vertical heat sink

Rohsenow and Cohen:
$$Sv_{OPT}(L_c) = 2.714 \cdot \frac{L_c}{Ra_L^{0.25}}$$

L_C is the characteristic length for Ra which is vertical height of the fins

Square Open Cavity: (a) All 3 walls isothermal (b) Wall facing opening isothermal, other adiabatic (c) partially open cavity

Applications are: (i) Solar thermal energy receivers (ii) Electronin Cooling Chambers

(In preparation)

Other correlations in Natural Convective with effects of Variable Properties & B.C.

Siebers et al:

$$Nu_{VPQ}(Gr_L) = \begin{cases} 0.404 (Gr_L)^{\frac{1}{4}} \cdot \left(\frac{T_A}{T_S}\right)^{0.04} & \text{if } Gr_L \leq 10^9 \\ 0.098 (Gr_L)^{\frac{1}{3}} \cdot \left(\frac{T_A}{T_S}\right)^{0.14} & \text{if } 10^9 < Ra_L \end{cases}$$

Plate surface at Uniform Heat Flux

$$Nu_{VPT}(Gr_L) = \begin{cases} 0.356 (Gr_L)^{\frac{1}{4}} \cdot \left(\frac{T_A}{T_S}\right)^{0.04} & \text{if } Gr_L \leq 10^9 \\ 0.098 (Gr_L)^{\frac{1}{3}} \cdot \left(\frac{T_A}{T_S}\right)^{0.14} & \text{if } 10^9 < Ra_L \end{cases}$$

Plate surface at Uniform Temperature

Symmetrically heated isothermal plates (Elenbass, 1942)

$$Nu_{PPT}(Ra_S, L, S) = \frac{Ra_S}{24} \cdot \frac{S}{L} \cdot \left(1 - e^{\left(\frac{-35}{Ra_S \cdot \frac{S}{L}}\right)^{0.75}}\right)$$

Suggested readings:

- Ramesh, N. and S.P. Venkateshan, Experimental study of natural convection in a square enclosure using differential interferometer, *Int. J. of Heat and Mass Transfer*, 2001. 44: p. 1107-1117
- Catton, I. Natural convection in enclosures, in *Proc. of 6th Int. Heat Transfer Conference*, 1978, Toronto, Canada.
- Bar-Cohen, A. and W.M. Rohsenow, Thermally optimum spacing of vertical natural convection cooled, parallel plates, *J. Heat Transfer*, 1984. 106.
- Elenbaas, W., Heat dissipation of parallel plates by free convection, *Physica*, 1942. 9.
- Kato, H., N. Nishiwaki, and M. Hirata, On the turbulent Heat Transfer by Free Convection from a Vertical Plate, *Int. J. heat and mass transfer*, 1968. 11.
- Macgregor, R.K. and A.P. Emery, Free convection through vertical plane layers: moderate and high Prandtl number fluids, *J. Heat Transfer*, 1969. 91.
- Hollands, K.G.T., et al., Free convection heat transfer across inclined air layers, *J. Heat Transfer*, 1976, 98: p. 189-193.
- Lankhorst, A.M., D. Angirasa, and C.J. Hoogendoorn, LDV Measurements of Buoyancy-Induced Flows in an Enclosure at High Rayleigh Numbers, *Experimental Thermal and fluid Science*, 1993. 6(1): p. 74-79.
- Schmidt, F.W., et al., A comparison of experimental and predicted results for laminar natural convection in an enclosure, *Int. J. Heat & Fluid Flow*, 1986. 7: p. 183-190.
- Bejan, A., A. Al-Homoud, and J. Imberger, Experimental study of high Rayleigh number convection in a horizontal cavity with different end temperatures, *Journal of Fluid Mechanics*, 1981. 109: p. 283-299.
- Vliet, G.C. and C.K. Liu, An Experimental Study of Turbulent Natural Convection Boundary Layers, *Journal of Heat Transfer*, 1969. 91(4): p. 517
- Siebers, D.L., R.F. Moffatt, and R.G. Schwind, Experimental, Variable Properties Natural-Convection from a Large, Vertical, Flat Surface, *Journal of Heat Transfer - Transactions of the ASME*, 1985. 107(1): p. 124-132.
- Azevedo, L.F.A. and E.M. Sparrow, Natural convection in open ended inclined channels. *J. Heat Transfer*, 1985. 107.
- Globe, S. and D. Dropkin, Natural convection heat transfer in liquids confined between two horizontal plates. *J. Heat Transfer*, 1959. 81C
- Graaf, G.A.D. and E.F.M.V.D. Held, The relation between the heat transfer and the convection phenomena in enclosed plane air layers. *Appl. Sci. Res.*, 1953. 3: p. 393-409.
- Ayyaswamy, P.S. and I. Catton, The boundary layer regime for natural convection in a differentially heated, tilted rectangular cavity. *J. Heat Transfer*, 1973. 95.
- Arnold, J.N., I. Catton, and D.K. Edwards, Experimental investigation of natural convection in inclined rectangular regions of differing aspect ratios. *J. Heat Transfer*, 1976. 98(1): p. 67-72.
- Eckert, E.R.G. and W.O. Carlson, Natural convection in an air layer enclosed between two vertical plates with different temperatures. *International Journal of Heat and Mass Transfer*, 1961. 2(1-2): p. 106-110